



Student Name:
Student No.:
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Question No. 1
Possible

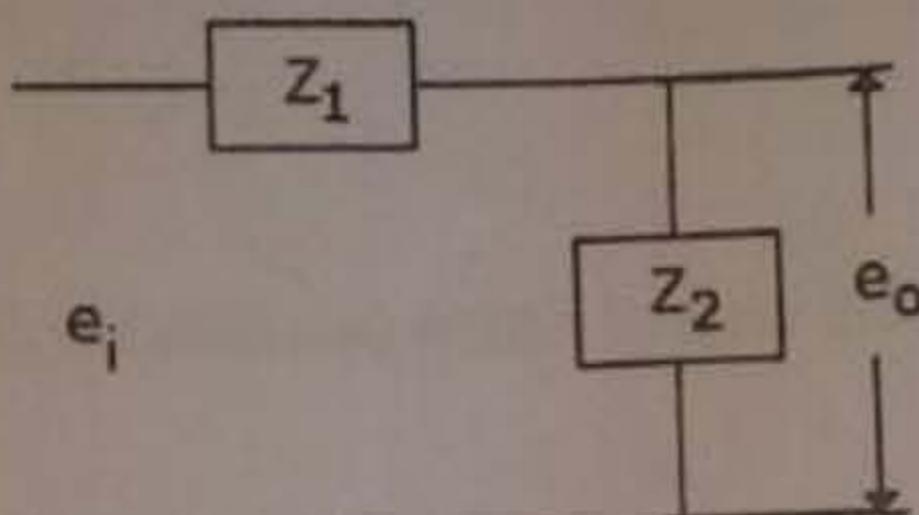
Choose the correct answer for the following (Show your work when)

1. A control system in which the control action is somehow dependent on the output is known as

- (a) Closed loop system
- (b) Semi-closed loop system
- (c) Open system
- (d) None of the above

2. For the system of the given figure the transfer function $\frac{E_o(s)}{E_i(s)} =$

(a) $\frac{Z_2(s)}{Z_1(s)}$

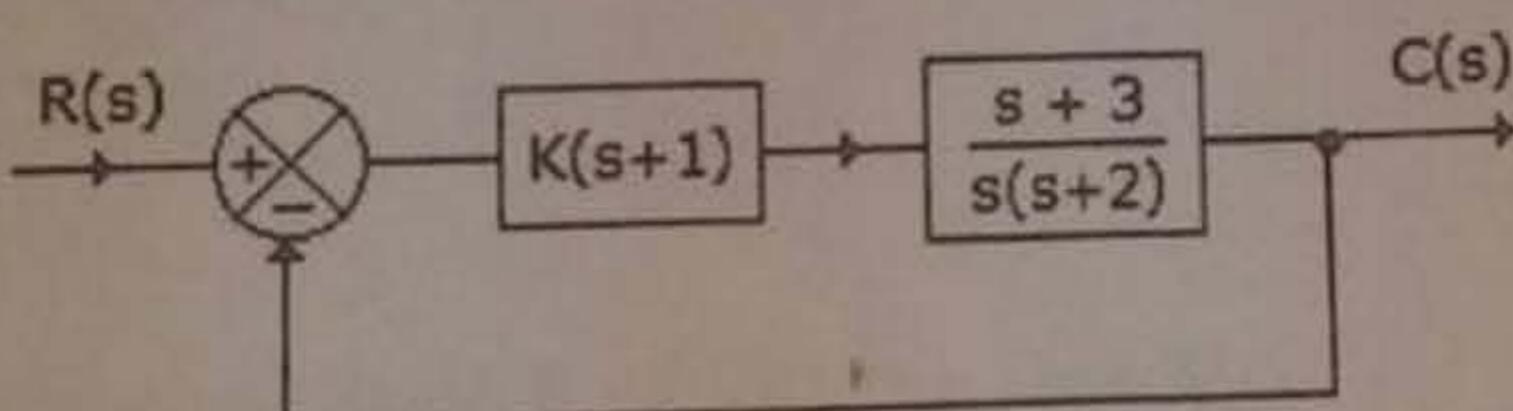


(b) $\frac{Z_2(s)}{Z_1(s) + Z_2(s)}$

(c) $\frac{Z_1(s)}{Z_2(s)}$

(d) $\frac{Z_1(s)}{Z_1(s) + Z_2(s)}$

3. For the system in the given figure the characteristic equation is



$$\frac{C(s)}{R(s)} = \frac{(K(s+1)) \left(\frac{s+3}{s(s+2)} \right)}{1}$$

(a) $1 + \frac{K(s+1)(s+3)}{s(s+2)} = 0$

(b) $1 + \frac{K(s-1)(s-3)}{s(s-2)} = 0$

(c) $K(s+1)(s+3) = 0$

(d) $s(s+2) = 0$

4. The first column of a Routh array is

s^5	1
s^4	2
s^3	1.5
s^2	-1/3
s^1	10
s^0	2

How many roots of the corresponding characteristic equation are in left half s -plane?

- (a) 2
- (c) 4

(b) 3

(d) 5

5. A signal other than the reference input that tends to affect the value of controlled known as

- (a) disturbance
- (b) command
- (c) control element
- (d) reference input

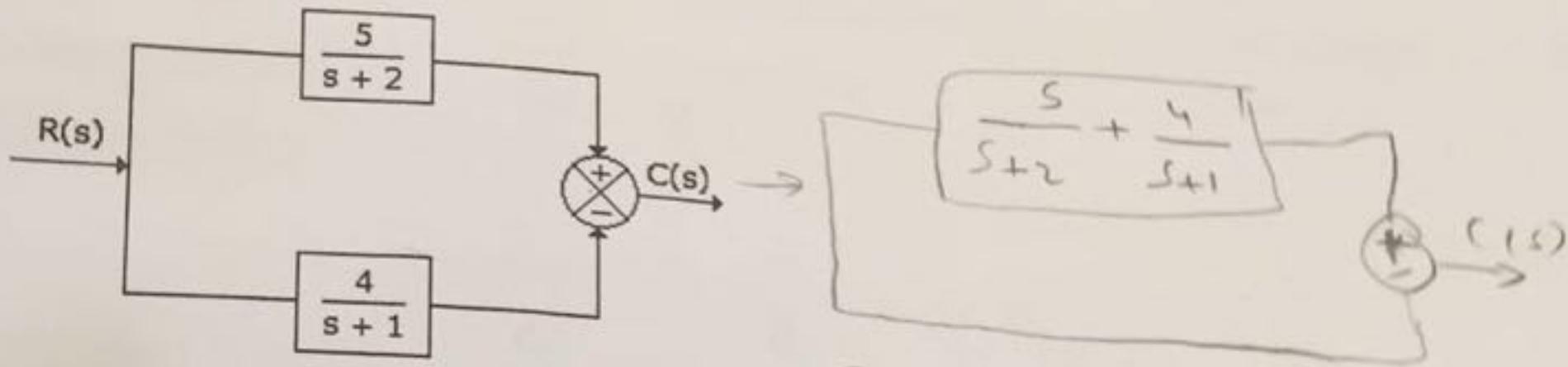
6. By which of the following the control action (actuator) is determined when a man along a path ?

- (a) Brain
- (b) Hands
- (c) Legs
- (d) Eyes

7. Which of the following is the input to a controller ?

- (a) Servo signal
- (b) Desired variable value
- (c) Error signal
- (d) Sensed signal

8. The system of the given figure



- (a) has two poles and one zero in left half plane
- (b) has two poles and one zero in right half plane
- (c) has two poles in left half plane and zero in right half plane
- (d) none of the above

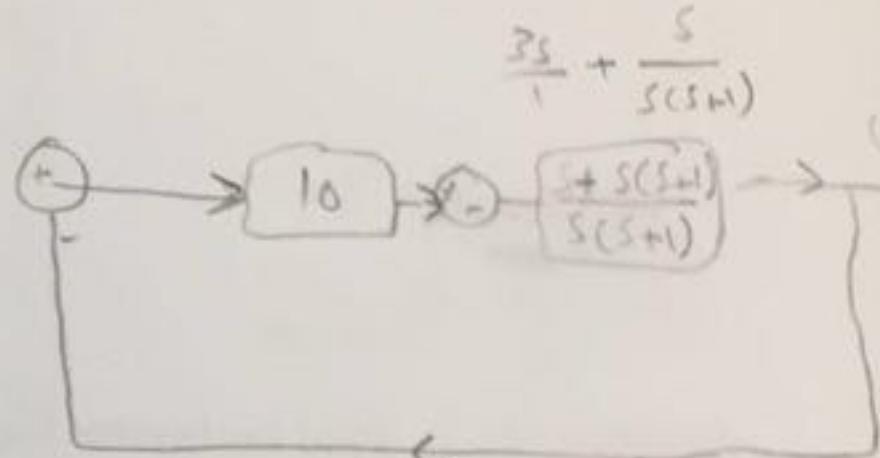
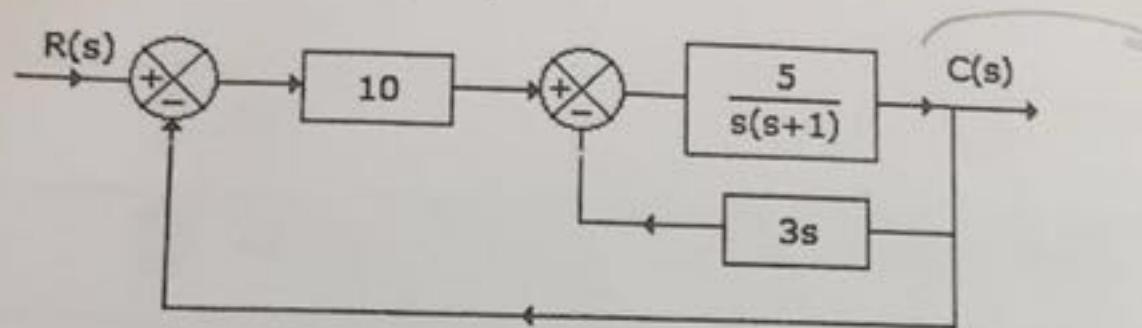
$$\frac{\text{Zero}}{\text{Poles}} = \frac{s(s+1) + 4(s+2)}{(s+2)(s+1)}$$

Locus

$$\frac{\text{Zero}}{\text{Poles}} = \frac{s^2 + 5s + 4}{s^2 + 3s + 2}$$

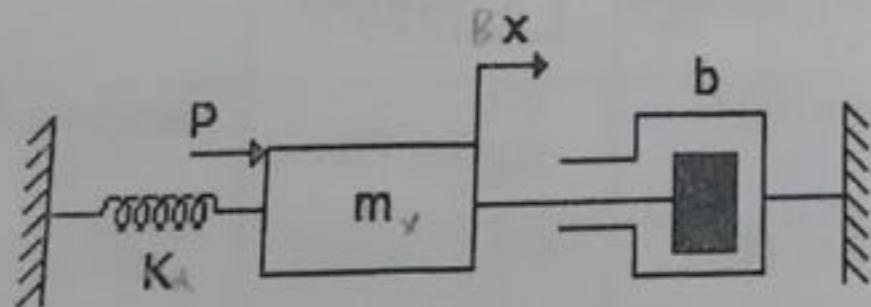
Poles

9. For the given figure, $\frac{C(s)}{R(s)} =$



- (a) $\frac{50}{s^2 + 50}$
- (b) $\frac{50}{s^2 + 16s + 50}$
- ~~(c)~~ $\frac{50}{s^2 + 4s + 50}$
- (d) $\frac{50}{s^2 + 16s}$

10. In the given figure, $P = 3$ kg force. Then $X(s) =$



- (a) $\frac{3}{ms + b + K}$
- (b) $\frac{3}{ms^2 + bs + K}$

- (c) $\frac{3}{s(ms^2 + bs + K)}$
- (d) $\frac{3}{s^2(ms^2 + bs + K)}$

mechanical system

① Free body diagram

$$\begin{cases} \textcircled{2} \sum F = ma \\ \textcircled{3} T.F \end{cases}$$

$$m\ddot{x} = -Kx - Bx + f$$

$$m\ddot{x} + Bx + Kx = f$$

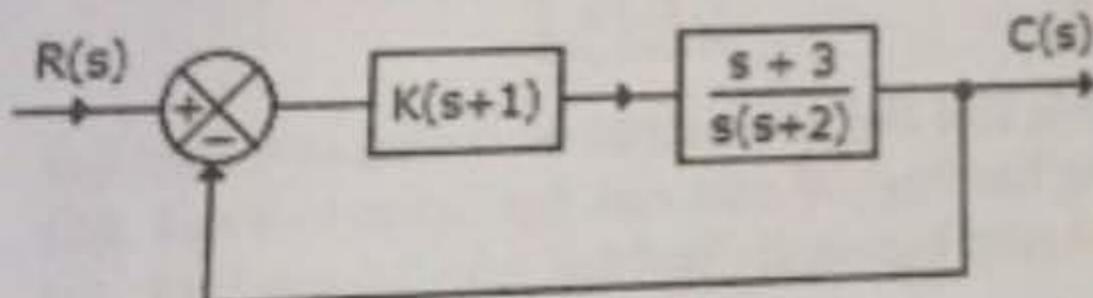


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Question No. 1 Choose the correct answer for the following (Show your work when Possible) (8 Marks)

1. A control system in which the control action is somehow dependent on the output is known as
 - Closed loop system
 - Semi-closed loop system
 - Open system
 - None of the above
2. The initial response when the output is not equal to input is called
 - Transient response
 - Error response
 - Dynamic response
 - Either of the above
- 3 - The position and acceleration errors of a type-2 system are
 - constant, constant
 - constant, infinity
 - zero, constant
 - zero, zero
4. For the system in the given figure the characteristic equation is



(a) $1 + \frac{K(s+1)(s+3)}{s(s+2)} = 0$

(b) $1 + \frac{K(s+1)(s+3)}{s(s+2)} = 0$

(c) $K(s+1)(s+3) = 0$

(d) $s(s+2) = 0$

5. The first column of a Routh array is

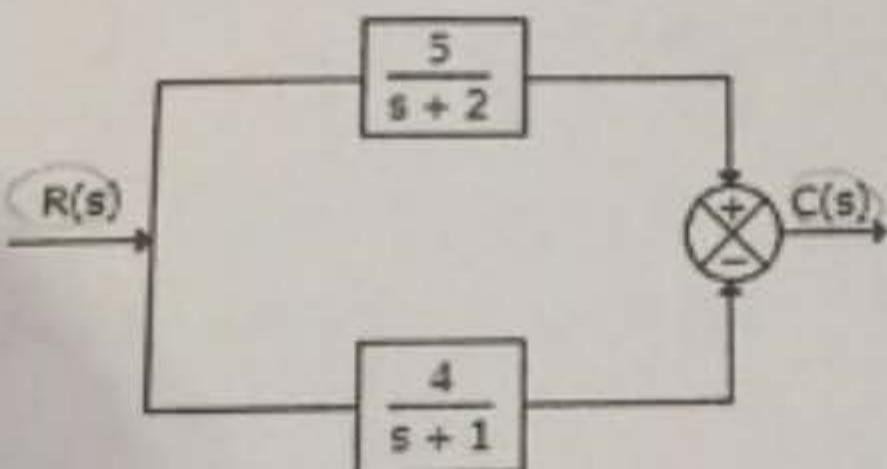
s^5	1
s^4	2
s^3	1.5
s^2	-1/3
s^1	10
s^0	2

How many roots of the corresponding characteristic equation are in left half s -plane?

6. A signal other than the reference input that tends to affect the value of controlled variable is known as:

- (a) disturbance
 - (b) command
 - (c) control element
 - (d) reference input

7. The system of the given figure



- (a) has two poles and one zero in left half plane
 - (b) has two poles and one zero in right half plane
 - (c) has two poles in left half plane and zero in right half plane
 - (d) none of the above

8. If the open loop transfer function of a unity feedback system is
then the poles of the closed loop system are at

- (a) -2, -2
 (b) -2, -1
 (c) -2, $\pm j$ 1
 (d) -2, 2

$$G(s) = \frac{1}{(s + 2)^2}$$

Question No. 4.2 A linear time-invariant system with input $r_1(t)$ and outputs $y_1(t)$ and $y_2(t)$ is described by the following set of differential equations. (30+15 Marks)

$$\frac{d^2y_1(t)}{dt^2} + 2\frac{dy_1(t)}{dt} + 3y_2(t) = r_1(t)$$

$$\frac{d^2y_2(t)}{dt^2} + 3\frac{dy_1(t)}{dt} + y_1(t) - y_2(t) = \frac{dr_1(t)}{dt}$$

* Find the transfer function $Y_1(s)/R_1(s)$ using the block diagram method ?

$$\textcircled{1} @ \text{Zeros} = s+2=0 \Rightarrow s=-2$$

Poles = $(s+3)^2 = 0$

\textcircled{a} $(s+3)(s+3) = 0 \Rightarrow s = -3, -3$

\textcircled{b} $s+6 \Rightarrow s = -6$

\textcircled{b} Time Response

$$y(t) = \lim_{s \rightarrow 0} s G(s) \frac{R}{s}$$

$$= \lim_{s \rightarrow 0} G(s)$$

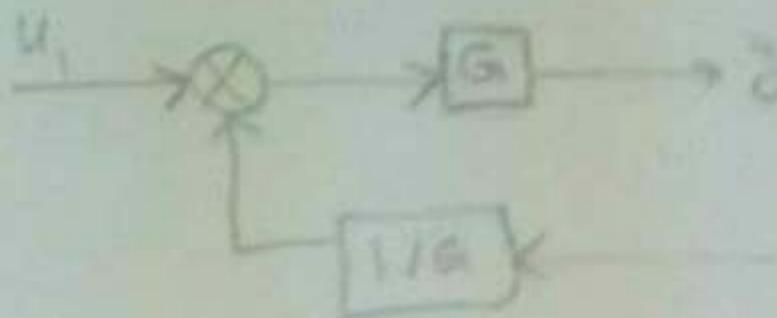
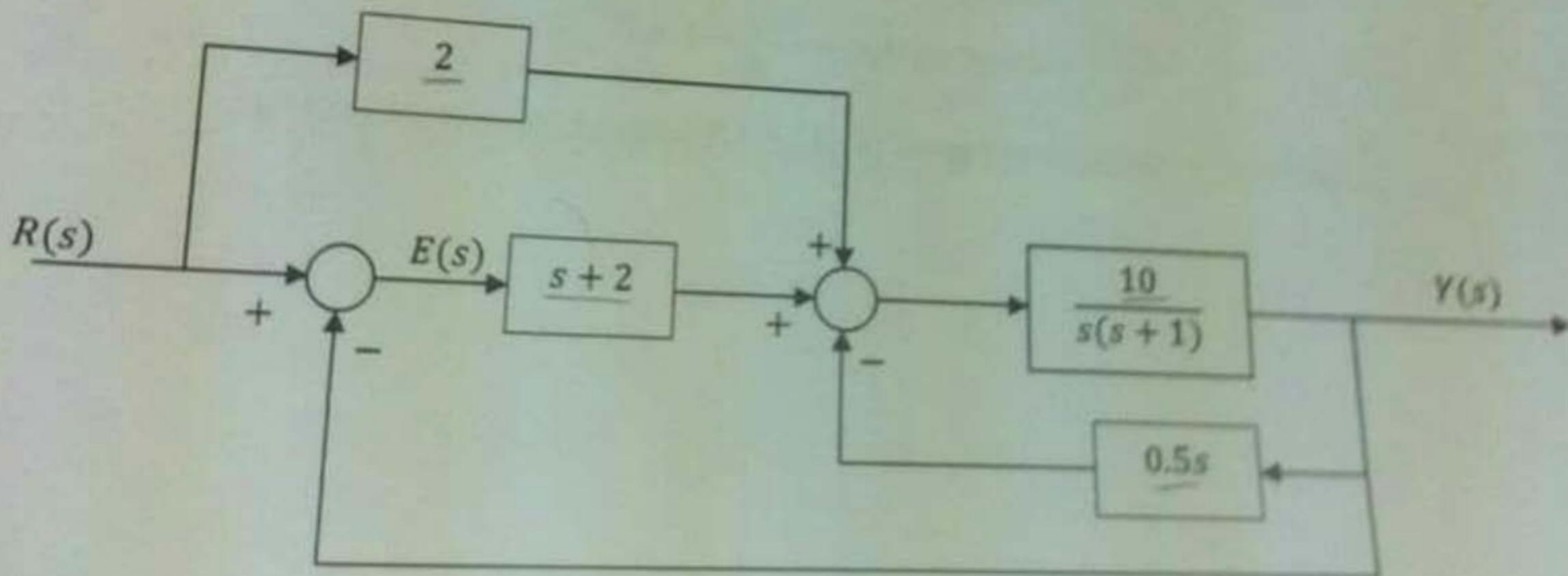
$$= G(0)$$

$$= \frac{0+2}{(0+3)^2(0+6)} = \frac{2}{(9)(6)} = \frac{2}{54}$$

والله أعلم

CHOOSE ONLY ONE OF THE FOLLOWING QUESTIONS (4.1 or 4.2)

Question No. 4.1 The Block diagram of a feedback system is shown below. Find the following transfer function: $\frac{Y(s)}{R(s)}$ (30 Marks)



A block diagram showing two input signals, u_1 and u_2 , entering a summing junction. The output of this junction is $e_n = 6(u_1 - u_2)$.

Sl. No.	Time Domain f(t)	S Domain F(s)
		$F(s) = \int_0^\infty e^{-st} f(t) dt$
1	Unit impulse $\delta(t)$	1
2	Unit step	$\frac{1}{s}$
3	t	$\frac{1}{s^2}$
4	t^n	$\frac{n!}{s^{n+1}}$
5	$f'(t)$	$sF(s) - f(0)$
6	$f''(t)$	$s^2 F(s) - sf(0) - f'(0)$
7	e^{at}	$\frac{1}{s-a}; s > a$
8	$t^n e^{at}$	$\frac{n!}{(s-a)^{n+1}}$
9	$\sin at$	$\frac{a}{s^2 + a^2}; s > 0$
10	$\cos at$	$\frac{s}{s^2 + a^2}; s > 0$
11	$\sinh at$	$\frac{a}{s^2 - a^2}; s > a $
12	$\cosh at$	$\frac{s}{s^2 - a^2}; s > a $
13	$e^{at} \sin bt$	$\frac{(s-a)^2 + b^2}{(s-a)}$
14	$e^{at} \cos bt$	$\frac{(s-a)^2 + b^2}{b}$
15	$e^{at} \sinh bt$	$\frac{(s-a)^2 - b^2}{(s-a)}$
16	$e^{at} \cosh bt$	$\frac{(s-a)^2 - b^2}{(s-a)}$
17	n th derivative	$s^n F(s) - s^{n-1} f(0) - s^{n-2} f'(0) - \dots - f^{n-1}(0)$
18	$\int_0^t f(\tau) d\tau$	$\frac{1}{s} F(s)$
19	$\int_0^t f(t-\tau) g(\tau) d\tau$	$F(s) G(s)$
20	$f(at)$	$\frac{1}{a} F\left(\frac{s}{a}\right)$
21	$e^{at} f(t)$	$F(s-a)$
22	$\delta(t-a)$	$\frac{1}{s} e^{-ax}$
23	t^{n-1}	$\frac{1}{s^n}; n = 1, 2, 3, \dots$
24	$\frac{(n-1)!}{t^{n-1}}$	$\frac{1}{(s+a)^n}; n = 1, 2, 3, \dots$
25	$\frac{1}{a^2} [1 - \cos at]$	$\frac{1}{s(s^2 + a^2)^2}$
26	$e^{-at} \sin \omega t$	$\frac{\omega}{(s+a)^2 + \omega^2}$



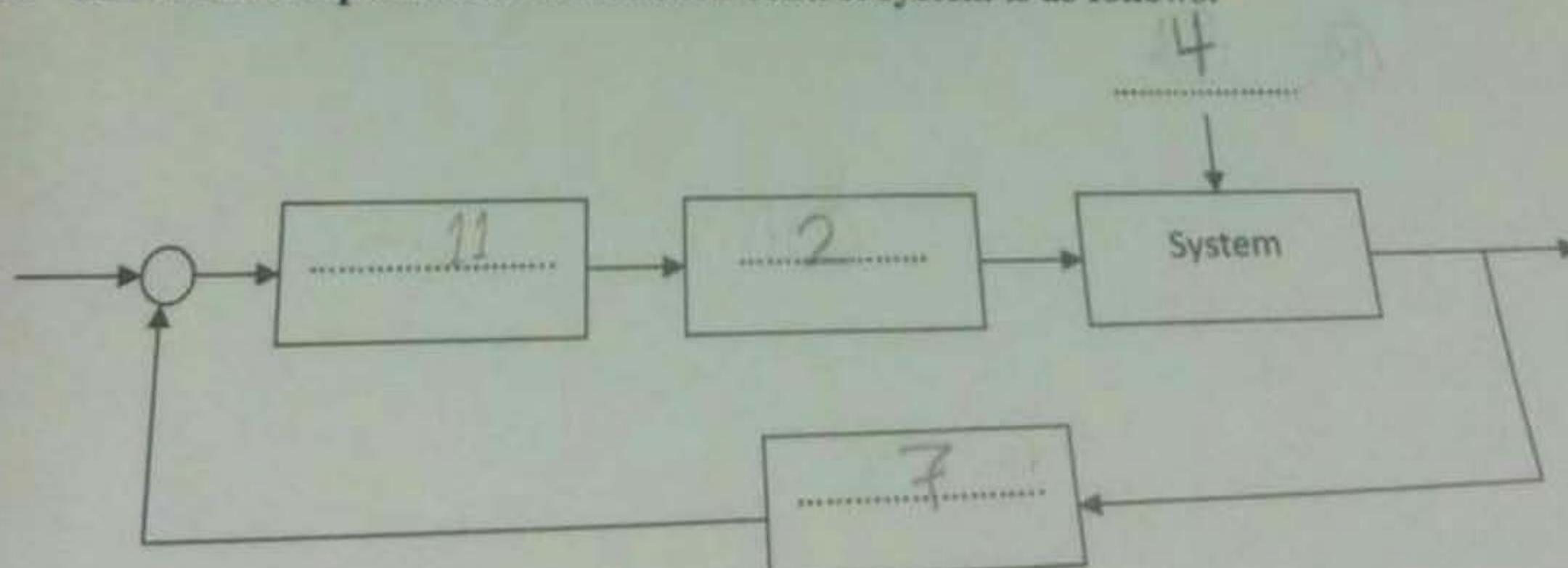
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Question No. 1 Choose the correct number and write it down in the blanks below (30 Marks)
(Words can be used more than once, others may be ignored)

1	algebraic	5	more	9	Output	13	ordinary differential
2	actuator	6	analysis	10	Design	14	Input
3	feedback	7	sensor	11	Controller	15	Poles
4	disturbance	8	zeros	12	Less	16	System

- Control is to make some object called 16 to behave as we desire.
- Laplace is used to transform an 13 equation to an 1 equation.
- A transfer function is defined by Laplace transform of system 9 divided by Laplace transform of the system 14
- A model is used for the 6 and 10 of control systems.
- Unstable systems have to be stabilized by 3
- The more time delay is, the 5 difficult it is to control.
- In control, 8 are the roots of the numerator.
- In control, 15 are the roots of the denominator.
- The main components of a feedback control system is as follows:



Question No. 3 For the following characteristic equations of feedback control systems, determine the range of K so that the system is stable. Find the frequency of oscillation if applicable. (20 Marks)

$$s^3 + 20s^2 + 5s + 10K = 0$$



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Question No. 2 The following differential equation represents a linear time-invariant system, where $r(t)$ denotes the input and $y(t)$ denotes the output. (30 Marks)

$$\ddot{y} + 12\dot{y} + 32y = \dot{r} + 5r$$

- Find the transfer function $Y(s)/R(s)$.
- If the input is a unit ramp function, obtain the solution $y(t)$ using the Laplace transform method. In other words, find the ramp response of the system.
- Using the transfer function in (a), find the steady-state error for a unit step input.

$$\ddot{y} + 12\dot{y} + 32y = \dot{r} + 5r$$

Question No. 4 Given the transfer function

$$G(s) = \frac{Y(s)}{U(s)} = \frac{4(s+1)}{s^2 + 3s + 2}$$

- a) What are the zeros of this transfer function?
- b) What are the poles of this transfer function?
- c) What is the partial fraction expansion of this transfer function?
- d) What is the impulse response associated with this transfer function (so far)?

a) Zeros $s+1 = 0 \Rightarrow s = -1$

b) Poles $s^2 + 3s + 2$
 $\alpha = 1$
 $b = 3$
 $c = 2$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\frac{-3 \pm \sqrt{9 - 4(1)(2)}}{2(1)}$$

$\therefore s = -1$ $s = -2$

$$(s+1)(s+2)$$

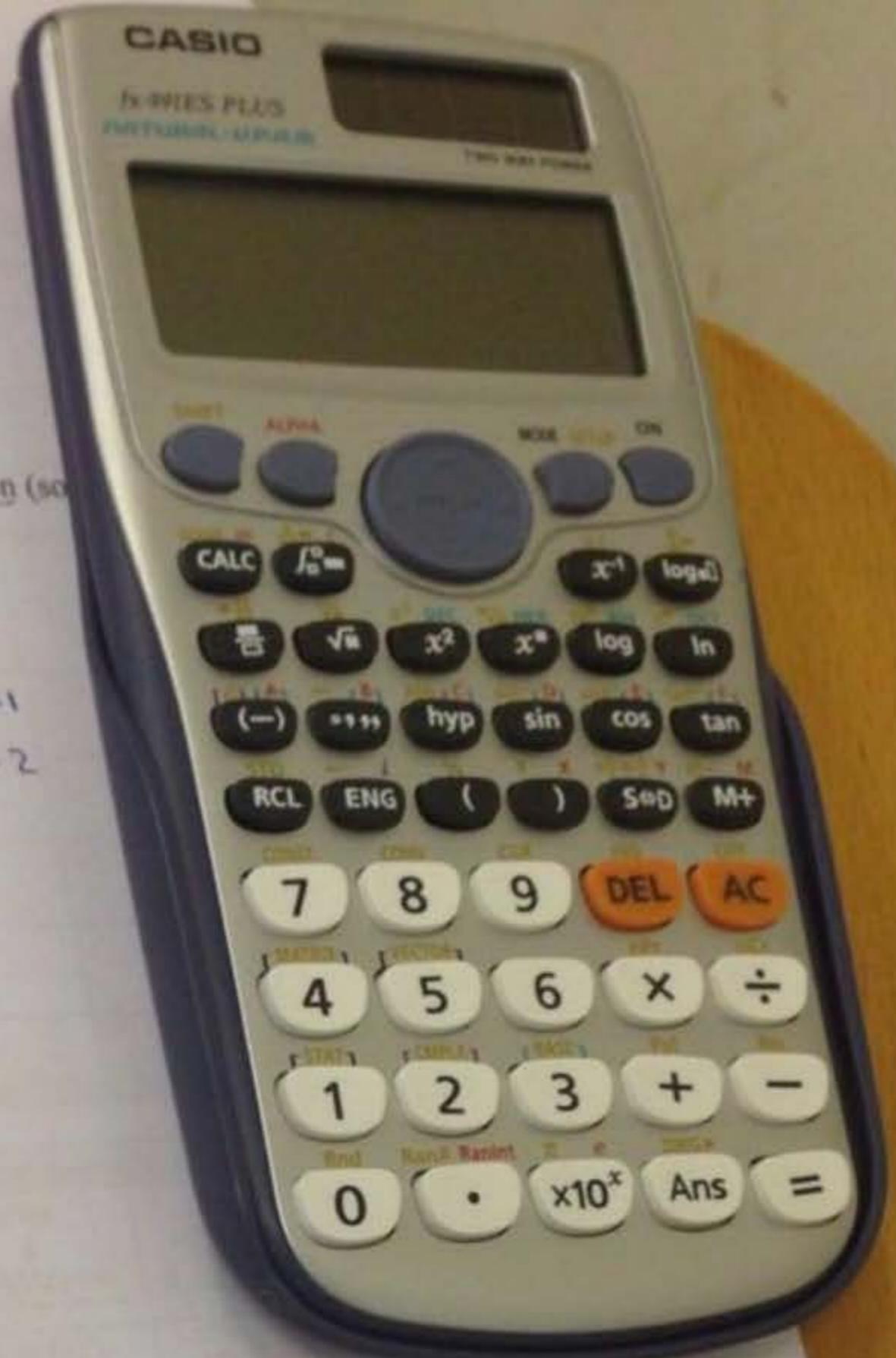
$$\frac{A}{s} - \frac{B}{s+1} - \frac{C}{s+2}$$

$$A = \frac{4(s+1)}{s^2 + 3s + 2} \Big|_{s=0}$$

$$\frac{4}{2} = 2$$

$$B = \frac{4(s+1)}{s^2 + 3s + 2} \Big|_{s=-1} = 0$$

$$C = \frac{4(s+1)}{s^2 + 3s + 2} \Big|_{s=-2} = -4$$



Question No. 4 Given the transfer function

$$G(s) = \frac{Y(s)}{U(s)} = \frac{4(s+1)}{s^2 + 3s + 2}$$

- a) What are the zeros of this transfer function?
- b) What are the poles of this transfer function?
- c) What is the partial fraction expansion of this transfer function?
- d) What is the impulse response associated with this transfer function (solve)?

@ Zeros

$$= 4(s+1) = 0$$

Zeros = -1

① Poles

$$= s^2 + 3s + 2 = 0$$

Poles = -1

Question No. 2 Find the Laplace Transform of the following function

$$e^{2t}(\sin 2t + 5t - 2)$$

~~Ans~~ ~~L~~ ~~s+2~~ ~~+ 5~~ ~~2~~ ~~5~~

~~Ans~~ ~~L~~ $\left(\frac{2}{s+4} + \frac{1}{s^2} - \frac{2}{s} \right)$

Question No. 3 Find the Inverse Laplace Transform of the following function

$$\frac{s+1}{s^2+4}$$

Find transfer Function

$$G(s) = \frac{C(s)}{R(s)} = \frac{(s+2)}{(s+3)^2 (s+6)}$$

- ① Where are the poles and zeros
- ② Determine the time response for a unit step input

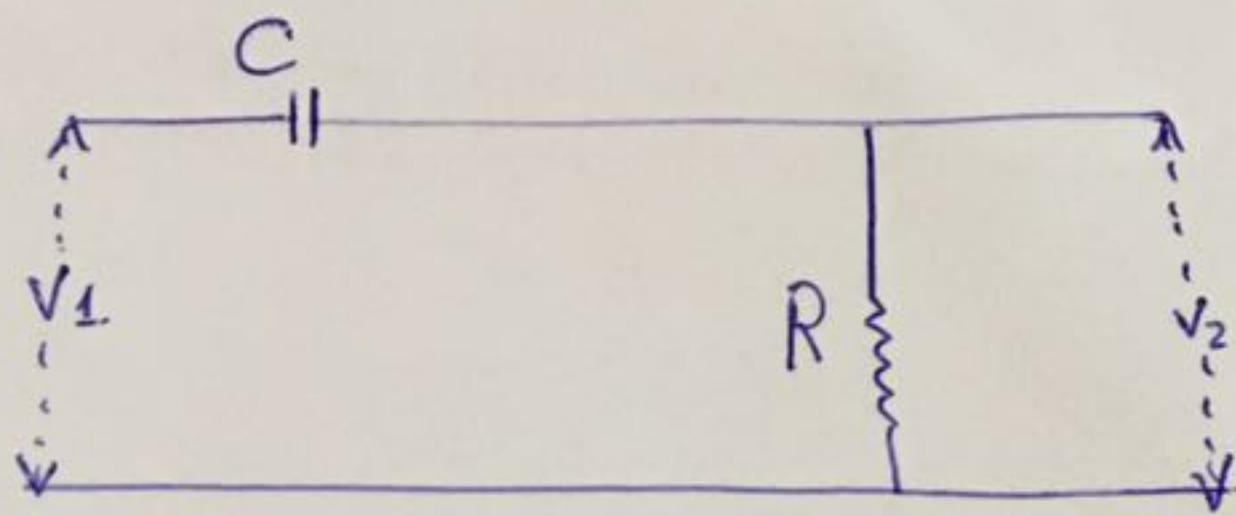
$$s^4 + 2s^3 + 15s^2 + 20s + K = 0$$

Determine the range of K so that the system is Marginally stable

$$s^3 + 20s^2 + 5s + 10K = 0$$

" " " K " " " " stable
System

- ① For Following Circuit Find transfer Function From $V_1(s)$ to $V_2(s)$.



$$V_i(t) = 10 \Rightarrow V_i(s) = \frac{10}{s}$$

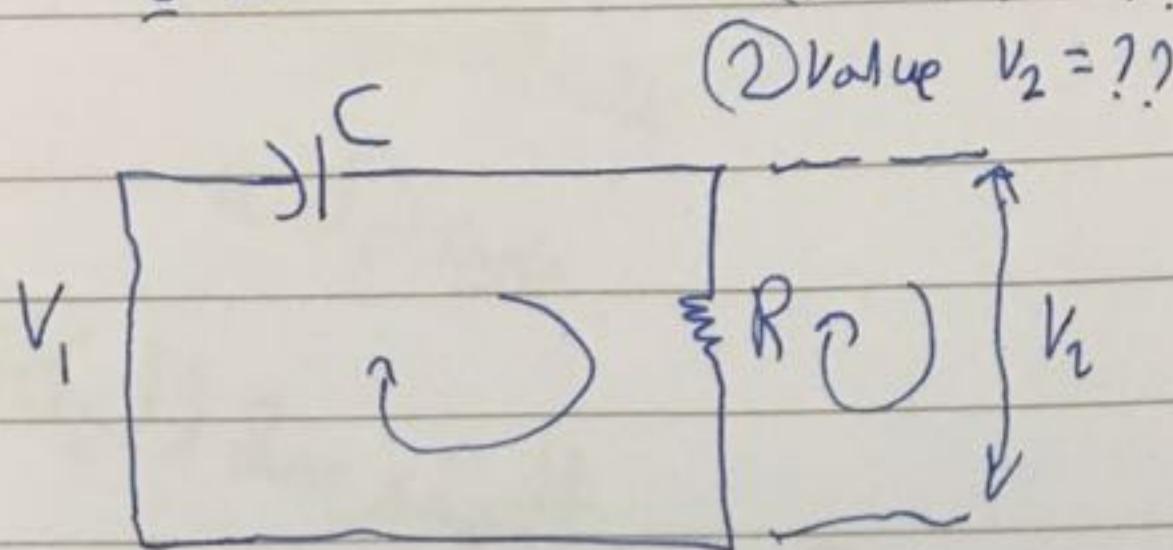
مخطى في الموارد

$$\textcircled{1} \quad TF = ??$$

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using Kirchhoff Law

$$V_i(s) = \frac{1}{C_s} + R$$

$$V_2(s) = R$$

$$\textcircled{1} \quad \therefore TF = \frac{V_2(s)}{V_i(s)} = \frac{R}{\frac{1}{C_s} + R} \\ = \frac{RC_s}{1 + RC_s}$$

$$\text{For } V_i(s) = \frac{10}{s} \Rightarrow V_2(s) = \frac{RC_s}{1 + RC_s} * \frac{10}{s}$$

$$= \frac{RC(10)}{1 + RCS}$$

\textcircled{2}

$$\lim_{s \rightarrow 0} sV_2(s) = \frac{sRC(10)}{1 + RCS}$$

$$= \frac{0}{1+0} = 0 \quad \Rightarrow$$

Consider the closed loop system given by

- (a) Determine the values ζ and ω_n that the system responds to a step input with approximately 16% overshoot and with a settling time 2 sec (assuming a response within 5% of the steady state value) Write the T.F of the system
- (b) Find the steady-state error the T.F Found in (a) For a unit step input

$$\frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2}$$

Feed Back تجلي و

$$\lim_{s \rightarrow 0} s Y(s)$$

$$s \rightarrow 0$$

$$A_1 + A_2 y + 32y = r + 5r$$

all

$$\frac{Y}{R} = ?$$

$$s^2 Y(s) + 12s Y(s) + 32Y(s) = s R(s) + 5 R$$

$$Y(s)(s^2 + 12s + 32) = R(s)(s + 5)$$

$$s + 5$$

If input = unit r

$$R(s) =$$

⑤ Root locus

$$G(s) = \frac{(2s + 12)}{2s(s + 3)}$$

فقرة بـ حلقة فيها مراجعة

الله يوفقكم ولا تنسوني من الدعاء

أخوكم / عبد الله الطوبوي