

**Question: 1.** Solve the differential equations

(a)  $y'' - 4y' - 5y = 0$

[5+5+5] (b)  $y'' - 10y' + 25y = 0$

(c)  $y'' - 2y' + 2y = 0$

**Question: 2** Determine whether the functions

[5]  $f_1(x) = \cos 2x, f_2(x) = 1, f_3(x) = \cos^2 x \quad -\infty < x < \infty$   
are linearly independent or linearly dependent.

**Question:3.** The function  $y_1 = x^4$  is a solution of the differential equation

[10]  $x^2 y'' - 7xy' + 16y = 0$ . Use the formula to find the second solution  
and hence find the general solution.

**Question:4.** Solve of the differential equation by using Variation of Parameter

[10]  $x^2 y'' - 2xy' + 2y = x^4 e^x$

**Question:5.** Use power series method to find the general solution of the

[10] differential equation  $(x^2 + 1)y'' + 2xy' = 0$ .